Course guide  
200901 - SAGDM - Seminar on Algebra, Geometry and Discrete Mathematics

Unit in charge: School of Mathematics and Statistics  
Teaching unit: 749 - MAT - Department of Mathematics.  
Degree: MASTER'S DEGREE IN ADVANCED MATHEMATICS AND MATHEMATICAL ENGINEERING (Syllabus 2010). (Optional subject).  
Academic year: 2022  
ECTS Credits: 3.0  
Languages: English

LECTURER

Coordinating lecturer: JUAN JOSÉ RUE PERNA  
Others: Segon quadrimestre: JUAN JOSÉ RUE PERNA - A

PRIOR SKILLS

The student must know the basics on graph theory. Additionally, it is necessary to have some knowledge on probability theory, group theory and arithmetics.

DEGREE COMPETENCES TO WHICH THE SUBJECT CONTRIBUTES

Specific:
MAMME-CE1. RESEARCH. Read and understand advanced mathematical papers. Use mathematical research techniques to produce and transmit new results.
MAMME-CE3. CALCULUS. Obtain (exact or approximate) solutions for these models with the available resources, including computational means.
MAMME-CE4. CRITICAL ASSESSMENT. Discuss the validity, scope and relevance of these solutions; present results and defend conclusions.

TEACHING METHODOLOGY

This seminar will be based on the presentation (from the responsible and the students) of material in the context of the theory of expanders. This material will be taken from specialized books and research papers.

LEARNING OBJECTIVES OF THE SUBJECT

The main objective of the seminar is to show an area of mathematics that intersects both algebra and geometry, discrete mathematics and other related areas, such as computer science, low-dimensional geometry and probability theory, among others.

The main objective is to get the student to gain a basic knowledge of expander theory, as well as the various applications in various branches of contemporary mathematics. In this direction, the student will also be encouraged to learn to conduct technical talks in public and in the preparation of technical scientific documents.
STUDY LOAD

<table>
<thead>
<tr>
<th>Type</th>
<th>Hours</th>
<th>Percentage</th>
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<tbody>
<tr>
<td>Hours large group</td>
<td>24.0</td>
<td>32.00</td>
</tr>
<tr>
<td>Self study</td>
<td>51.0</td>
<td>68.00</td>
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</tbody>
</table>

Total learning time: 75 h

CONTENTS

Spectral graph Theory and expanders

Description:
- Spectral graph theory.

Full-or-part-time: 20h
Theory classes: 6h 40m
Self study : 13h 20m

Graph expanders and group theory

Description:
- Cayley graphs. Properties
- Random walks in Cayley graphs.
- Kazhan Property (T) and relation with expansion phenomena

Full-or-part-time: 9h 20m
Theory classes: 6h
Self study : 3h 20m

Graf expanders and Number Theory

Description:
- Classical algebraic groups and quasi-random groups.
- Expansion in SL2(Fq): Helfgott Theorem and Bourgain-Gamburd

Full-or-part-time: 12h
Theory classes: 6h
Self study : 6h
Other applications of graph expanders

Description:
- Applications in knot theory: the Barzdin-Kolmogorov theorem
- Applications in theoretical computer science: design of concentrators
- Applications in theoretical computing: design of algorithms
- Applications in algebraic number theory: elliptic curves

Full-or-part-time: 12h
Theory classes: 6h
Self study: 6h

GRADING SYSTEM

The grading of this seminar will be based on three points: (CA) Continuous evaluation, (MP) Material preparation and (PT) presentation.

(CA): will be based on the understanding of the material, as well as the meetings that will be held between the student and the responsible to prepare the student’s presentation (or presentations). It will also include the fact of being active during the seminar sessions.

(MP): preparation of both the presentation, its good preparation and the summary sheet.

(PT): presentation. This will include questions from the teacher and students.

Overall grading of the seminar: 30% (CA) + 20% (MP) + 50% (PT)

BIBLIOGRAPHY

Basic:
- Davidoff,Giuliana; Sarnak, Peter; Valette, Alain. Elementary number theory, group theory and Ramanujan graphs [on line]. London Mathematical Society, 2003 Available on: https://doi.org/10.1017/CBO9780511615825.

Complementary: