Course guide
34953 - NT - Number Theory

Unit in charge: School of Mathematics and Statistics
Teaching unit: 749 - MAT - Department of Mathematics.
Degree: MASTER'S DEGREE IN ADVANCED MATHEMATICS AND MATHEMATICAL ENGINEERING (Syllabus 2010).
(Optional subject).
Academic year: 2023  ECTS Credits: 7.5  Languages: English

LECTURER

Coordinating lecturer: JOAN CARLES LARIO LOYO
Others: Primer quadrimestre:
JOAN CARLES LARIO LOYO - A
BERNAT PLANS BERENGUER - A

PRIOR SKILLS

Basic knowledge of algebraic structures: groups, rings and fields.

REQUIREMENTS

Basic material covered in any standard courses on arithmetic, group theory and Galois theory.

DEGREE COMPETENCES TO WHICH THE SUBJECT CONTRIBUTES

Specific:
1. RESEARCH. Read and understand advanced mathematical papers. Use mathematical research techniques to produce and transmit new results.
2. CALCULUS. Obtain (exact or approximate) solutions for these models with the available resources, including computational means.
3. CRITICAL ASSESSMENT. Discuss the validity, scope and relevance of these solutions; present results and defend conclusions.

Transversal:
4. SELF-DIRECTED LEARNING. Detecting gaps in one's knowledge and overcoming them through critical self-appraisal. Choosing the best path for broadening one's knowledge.
5. EFFICIENT ORAL AND WRITTEN COMMUNICATION. Communicating verbally and in writing about learning outcomes, thought-building and decision-making. Taking part in debates about issues related to the own field of specialization.
6. THIRD LANGUAGE. Learning a third language, preferably English, to a degree of oral and written fluency that fits in with the future needs of the graduates of each course.
7. TEAMWORK. Being able to work as a team player, either as a member or as a leader. Contributing to projects pragmatically and responsibly, by reaching commitments in accordance to the resources that are available.
8. EFFECTIVE USE OF INFORMATION RESOURCES. Managing the acquisition, structure, analysis and display of information from the own field of specialization. Taking a critical stance with regard to the results obtained.

TEACHING METHODOLOGY

Most of the lectures will take place on the blackboard (replaced by online lessons if necessary), explaining carefully the contents of the course and providing as much explicit examples, exercises and applications as possible. The students will be encouraged to consult suitable references and to discuss between them and with the professor in order to achieve a good understanding of the material.
LEARNING OBJECTIVES OF THE SUBJECT

1) Algebraic number theory.
2) Number theory in function fields.
2) Cyclotomic theory.

STUDY LOAD

<table>
<thead>
<tr>
<th>Type</th>
<th>Hours</th>
<th>Percentage</th>
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<tbody>
<tr>
<td>Self study</td>
<td>127.5</td>
<td>68.00</td>
</tr>
<tr>
<td>Hours large group</td>
<td>60.0</td>
<td>32.00</td>
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</tbody>
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Total learning time: 187.5 h

CONTENTS

**Algebraic Number Theory**

**Description:**
Introduction
Cyclotomic extensions
Cyclotomic polynomials

**Full-or-part-time:** 10h
Theory classes: 10h

**Number Theory in function fields**

**Description:**
Functions fields over finite fields
Carlitz polynomials
Carlitz extensions

**Full-or-part-time:** 10h
Theory classes: 10h
Cyclotomic Theory

Description:
- Cyclotomic integers
- Cyclotomic units
- Unique factorization
- Class numbers
- Galois action
- Kronecker-Weber theorem
- Regular polygons
- Fermat equation
- Quadratic reciprocity
- Carlitz modules
- Galois action
- Carlitz-Hayes theorem
- Cyclotomic and Carlitz analogies
- Quadratic reciprocity
- Drinfeld modules

Full-or-part-time: 40h
Theory classes: 40h

GRADING SYSTEM

There will be a final exam.

EXAMINATION RULES.

Solved exercises and works must be delivered according to schedule.

BIBLIOGRAPHY

Basic:
RESOURCES

Computer material:
- SAGE. Mathematical Software
- Matlab. Mathematical software