Course guides
34957 - GT - Graph Theory

Unit in charge: School of Mathematics and Statistics
Teaching unit: 749 - MAT - Department of Mathematics.

Degree: MASTER'S DEGREE IN ADVANCED MATHEMATICS AND MATHEMATICAL ENGINEERING (Syllabus 2010).
(Optional subject).

Academic year: 2021  ECTS Credits: 7.5  Languages: English

LECTURER

Coordinating lecturer: GUILLEM PERARNAU LLOBET

Others: Primer quadrimestre:
MARCOS NOY SERRANO - A
GUILLEM PERARNAU LLOBET - A
ORIOL SERRA ALBO - A

PRIOR SKILLS

Elementary Calculus and Linear Algebra; basic notions and skills in combinatorics and probability.

DEGREE COMPETENCES TO WHICH THE SUBJECT CONTRIBUTES

Specific:
1. RESEARCH. Read and understand advanced mathematical papers. Use mathematical research techniques to produce and transmit new results.
2. CALCULUS. Obtain (exact or approximate) solutions for these models with the available resources, including computational means.
3. CRITICAL ASSESSMENT. Discuss the validity, scope and relevance of these solutions; present results and defend conclusions.

Transversal:
4. SELF-DIRECTED LEARNING. Detecting gaps in one's knowledge and overcoming them through critical self-appraisal. Choosing the best path for broadening one's knowledge.
5. EFFICIENT ORAL AND WRITTEN COMMUNICATION. Communicating verbally and in writing about learning outcomes, thought-building and decision-making. Taking part in debates about issues related to the own field of specialization.
6. THIRD LANGUAGE. Learning a third language, preferably English, to a degree of oral and written fluency that fits in with the future needs of the graduates of each course.
7. TEAMWORK. Being able to work as a team player, either as a member or as a leader. Contributing to projects pragmatically and responsibly, by reaching commitments in accordance to the resources that are available.
8. EFFECTIVE USE OF INFORMATION RESOURCES. Managing the acquisition, structure, analysis and display of information from the own field of specialization. Taking a critical stance with regard to the results obtained.

TEACHING METHODOLOGY

Combination of theoretical lectures and exercise classes, with student presenting their solutions to the proposed problems. The active participation of students is a requirement for the course assessment.
LEARNING OBJECTIVES OF THE SUBJECT

Extremal graph theory
Application of spectral techniques to the study of graphs.
Application of the probabilistic method.
Properties of almost all graphs.
Properties of Cayley and vertex symmetric graphs.
Graphs on surfaces.
Minors.

STUDY LOAD

<table>
<thead>
<tr>
<th>Type</th>
<th>Hours</th>
<th>Percentage</th>
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<tbody>
<tr>
<td>Self study</td>
<td>127.5</td>
<td>68.00</td>
</tr>
<tr>
<td>Hours large group</td>
<td>60.0</td>
<td>32.00</td>
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</tbody>
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Total learning time: 187.5 h

CONTENTS

**Spectral techniques in Graph Theory**

**Description:**

**Specific objectives:**

**Full-or-part-time:** 12h
Theory classes: 12h

**Graphs symmetries**

**Description:**
Vertex symmetric and edge symmetric graphs. Cayley graphs. Highly symmetric graphs.

**Specific objectives:**

**Full-or-part-time:** 1h
Theory classes: 1h

**Minors and treewidth**

**Description:**

**Specific objectives:**
Classes defined by forbidden minors. Serie-Parallel graphs. k-trees and treewidth.

**Full-or-part-time:** 11h
Theory classes: 11h
Graphs on surfaces

**Description:**

**Specific objectives:**
Euler formula. Planar separator theorem

**Full-or-part-time:** 4h
Theory classes: 4h

Graph homomorphisms

**Description:**
Graph homomorphisms. Retracts and Cores. The homomorphism order. Antichains.

**Specific objectives:**
Homomorphisms and colorings. Fractional and circular chromatic numbers.

**Full-or-part-time:** 6h
Theory classes: 6h

Random graphs

**Description:**

**Specific objectives:**
Graphs with large girth and large chromatic number. Expansion properties of random graphs. Threshold for connectivity. The Poisson paradigm.

**Full-or-part-time:** 12h
Theory classes: 12h

Extremal Graph Theory

**Description:**

**Specific objectives:**
Counting Lemma and Removal Lemma. Applications of Szemerédi regularity Lemma.

**Full-or-part-time:** 12h
Theory classes: 12h

**GRADING SYSTEM**

The course assessment will be based on the weekly work on the proposed problems and their presentation during the lectures. There will be a final comprehensive exam on the course topics.
EXAMINATION RULES.

The active participation in the course is a requirement for the evaluation of the final exam.

BIBLIOGRAPHY

Basic:
- Alon, Noga; Spencer Joel. The Probabilistic Method. 2016. Wiley,

Complementary: